

Prof. Dr. Burkhard Stiller, Universität Zürich, Binzmühlestrasse 14, CH-8050 Zürich  
Telefon: +41 44 635 6710, Fax: +41 44 635 6809, stiller@ifi.uzh.ch  
Eder John Scheid, Telefon: +41 44 635 7586, scheid@ifi.uzh.ch  
Sina Rafati, Telefon: +41 44 635 6702, rafati@ifi.uzh.ch

## Exercise Sheet 2

### Computer Engineering and Communication Networks

Handout: 04.10.2018  
Discussion: 11.10.2018

#### 1. Arithmetics

- 1.1. Sum up the binary numbers  $10011_2$  and  $1011_2$ .
- 1.2. Subtract  $1010_2$  from  $1111_2$ .
- 1.3. Convert the number  $001111_2$  to its two's complement representation and then subtract it from  $011010_2$ .
- 1.4. Multiply the two binary numbers  $1011_2$  and  $1001_2$ .
- 1.5. Multiply the two binary numbers  $00001111_2$  and  $10000000_2$ .
- 1.6. Divide the binary number  $101101_2$  by  $1001_2$ .
- 1.7. Divide the binary number  $1111_2$  by  $0101_2$
- 1.8. Tick the correct answer to the questions below. Only one answer is correct.

Question 1: Which of the following binary numbers equals the two's complement representation (6 Bit length) of the decimal number  $-20_{10}$ ?

- $101011_2$
- $101100_2$
- $101010_2$
- none of the above

Question 2: In which number representation only one representation for the number zero exists?

- Representation absolute value plus algebraic sign
- One's complement
- Offset-Dual representation

Question 3: Which of the following binary numbers equals the offset-dual representation (5 Bit length) of the decimal number  $5_{10}$ ?

- $10101_2$   
  $00101_2$   
  $10100_2$   
 none of the above

## 2. Combinatorial Circuits

2.1. Derive from the Boolean Algebra the following absorption laws using the axioms shown on slides M3-7/8. State in each step, which one was used.

2.1.1.  $(a \wedge b) \vee (a \wedge \bar{b}) = a$

2.1.2.  $(a \vee \bar{b}) \wedge b = a \wedge b$

2.2. Find the **Disjunctive Normal Form (DNF)** and **Conjunctive Normal Form (CNF)** of the truth table below:

a	b	c	Result	Minterm	Maxterm
0	0	0	0		
0	0	1	1		
0	1	0	1		
0	1	1	1		
1	0	0	0		
1	0	1	0		
1	1	0	1		
1	1	1	0		

**DNF:**

**CNF:**

2.3. Convert the given Boolean equation  $y = a \wedge \bar{c} \vee b \wedge c$  into a NAND system.

2.4. Prove by using a truth table if the Boolean expression  $((a \rightarrow b) \wedge (b \rightarrow c)) \rightarrow (a \rightarrow c)$  represents a tautology, a contradiction, or nothing of all.

Truth Table for  $(A \rightarrow B)$ :

A	B	$A \rightarrow B$
0	0	1
0	1	1
1	0	0
1	1	1